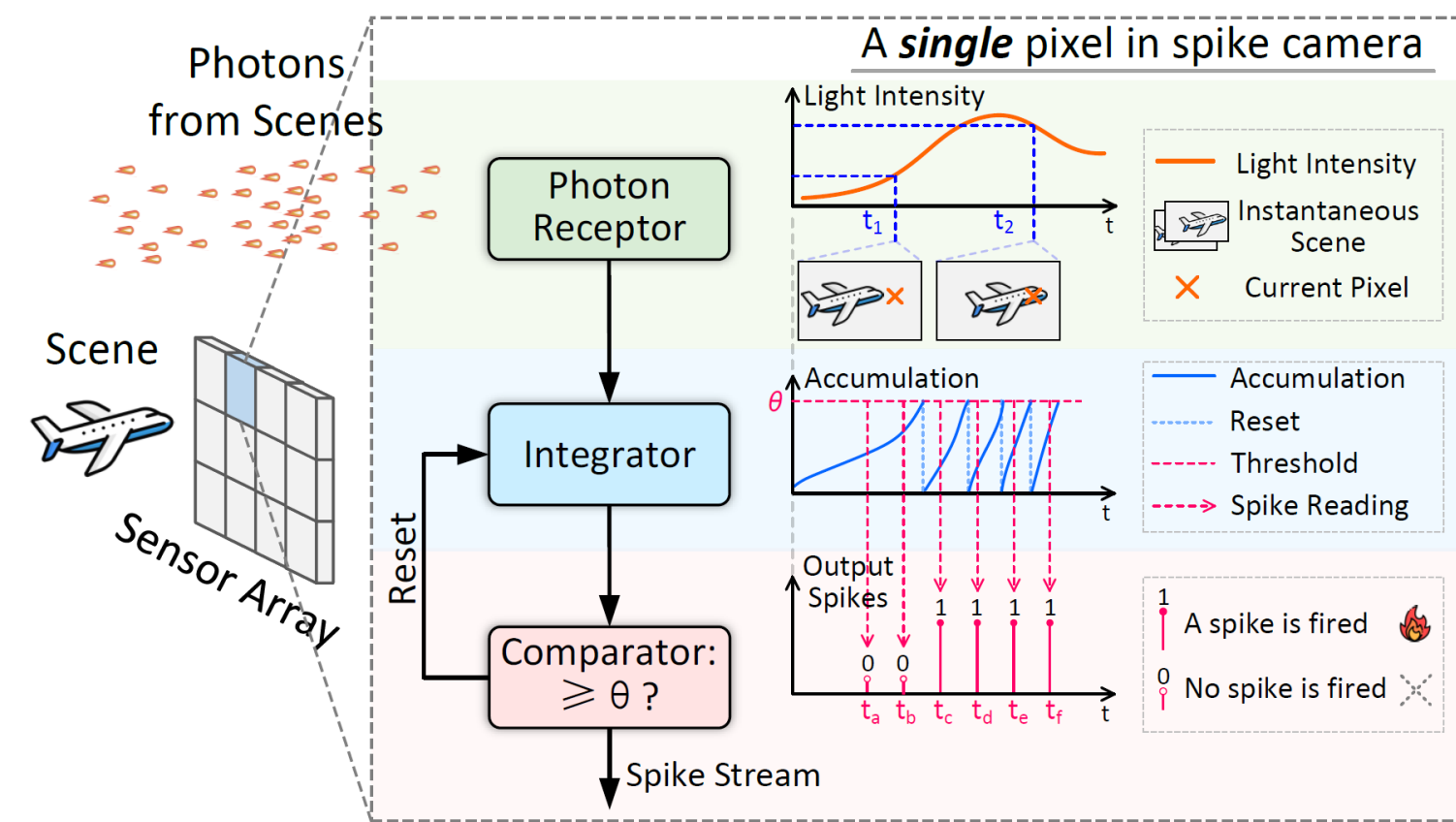


1. Introduction

1.1 Spike Camera Each pixel of the spike camera comprises three main components: a photon receptor, an integrator, and a comparator. The incoming photons are captured by the photon receptor and accumulated by the integrator. Whenever the number of accumulated photons reaches a predefined threshold θ , a spike is fired, and the integrator is reset.



Key components of a pixel in spike camera

$$A(\mathbf{x}, t) = \int_0^t \alpha \mathcal{P}(\mathbf{L}(\mathbf{x}, \tau)) d\tau \bmod \theta$$

α is the quantum conversion coefficient of photons. \mathcal{P} means Poisson sampling. $\mathbf{L}(\mathbf{x}, \tau)$ is the expected number of arrival photons at a pixel area per unit time.

1.2 Fluctuations in Spikes

Effects in the imaging of spike cameras.

- (a) Poisson Effect of Photons' Arrival
- (b) Quantitative effect from spike readout
- (c) Thermal noises in the circuits

Randomness in imaging procedure

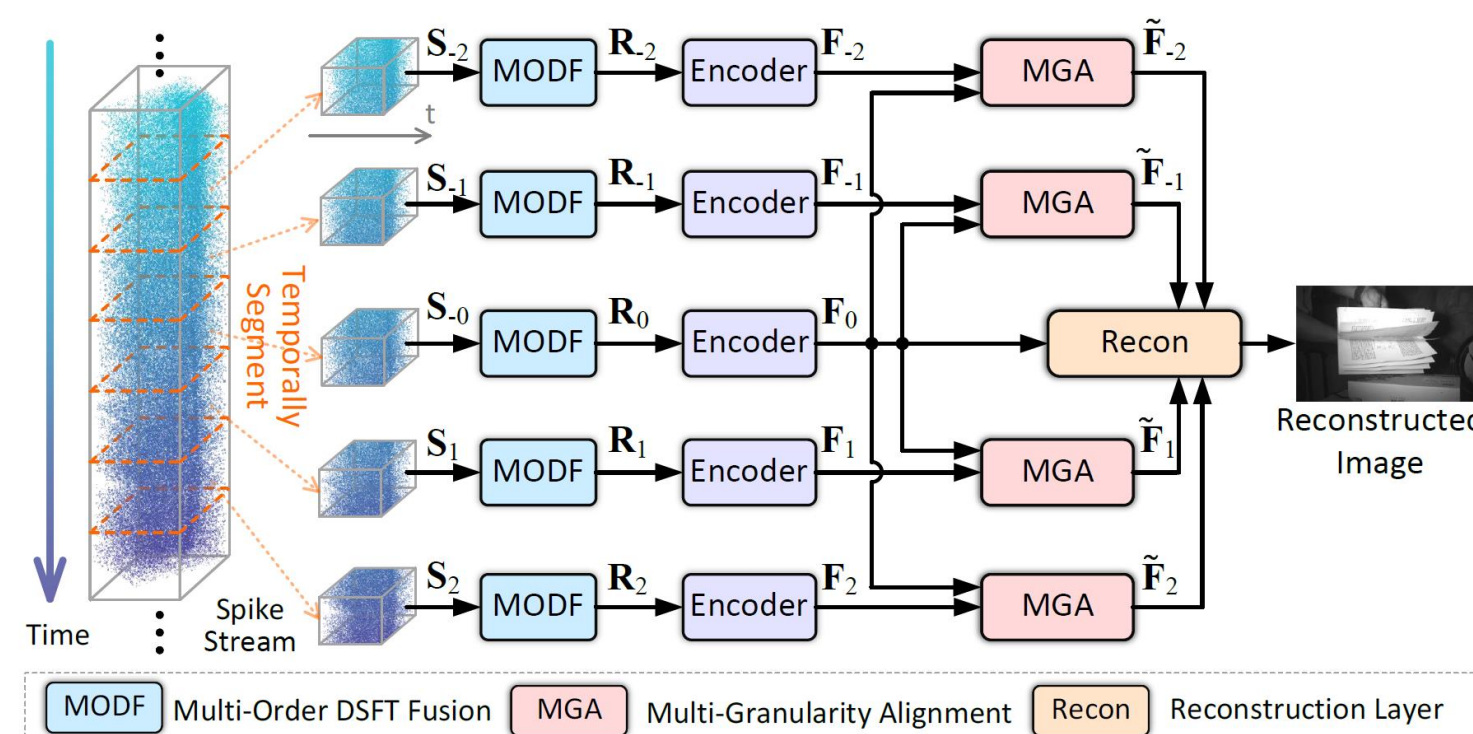
Integration period of spikes

Light intensity

Fluctuations: even when the light intensity is constant, the integration period of each spike changes over time.

2. Methods

2.1 Overall Architecture of the proposed method (BSF)



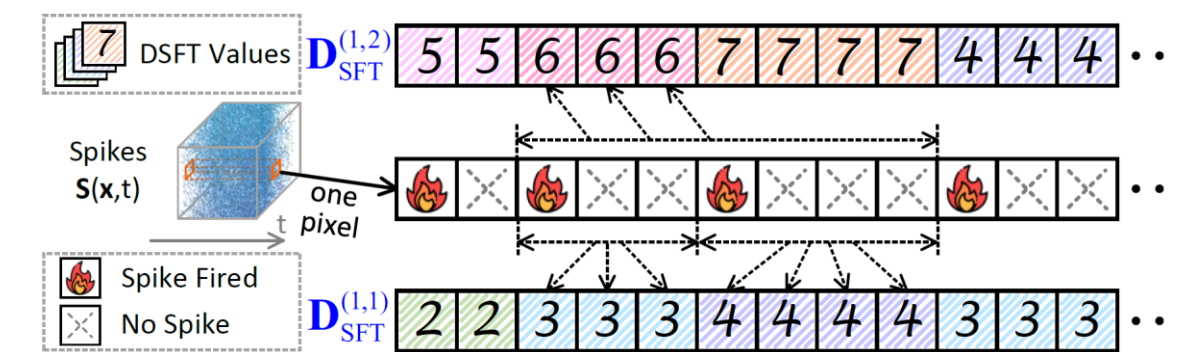
2. Methods

2.2 Multi-Order DSFT Fusion (MODF)

Proposition 1: Use DSFT as input.

DSFT: Differential of Spike Firing Time.

(1,1)-order DSFT, i.e., $D_{SFT}^{(1,1)}$



Proposition 2: Processing DSFT in reciprocal domain.

Theorem: When the photons' arrival is constant

$$\Pr\{D_{SFT}^{(1,1)} = \lceil \theta/L \rceil\} = p_1 = (\lceil \theta/L \rceil - \theta/L) \cdot \frac{\lceil \theta/L \rceil}{\theta/L}$$

$$\Pr\{D_{SFT}^{(1,1)} = \lfloor \theta/L \rfloor\} = p_2 = (\theta/L - \lfloor \theta/L \rfloor) \cdot \frac{\lfloor \theta/L \rfloor}{\theta/L}$$

$$\mathbb{E}\left(\frac{1}{D_{SFT}^{(1,1)}}\right) = \frac{1}{\lceil \theta/L \rceil} \cdot p_1 + \frac{1}{\lfloor \theta/L \rfloor} \cdot p_2 = \frac{L}{\theta}$$

The reciprocal of DSFT corresponds to unbiased estimation of light intensity

Proposition 3: Fusing DSFT with multiple orders.

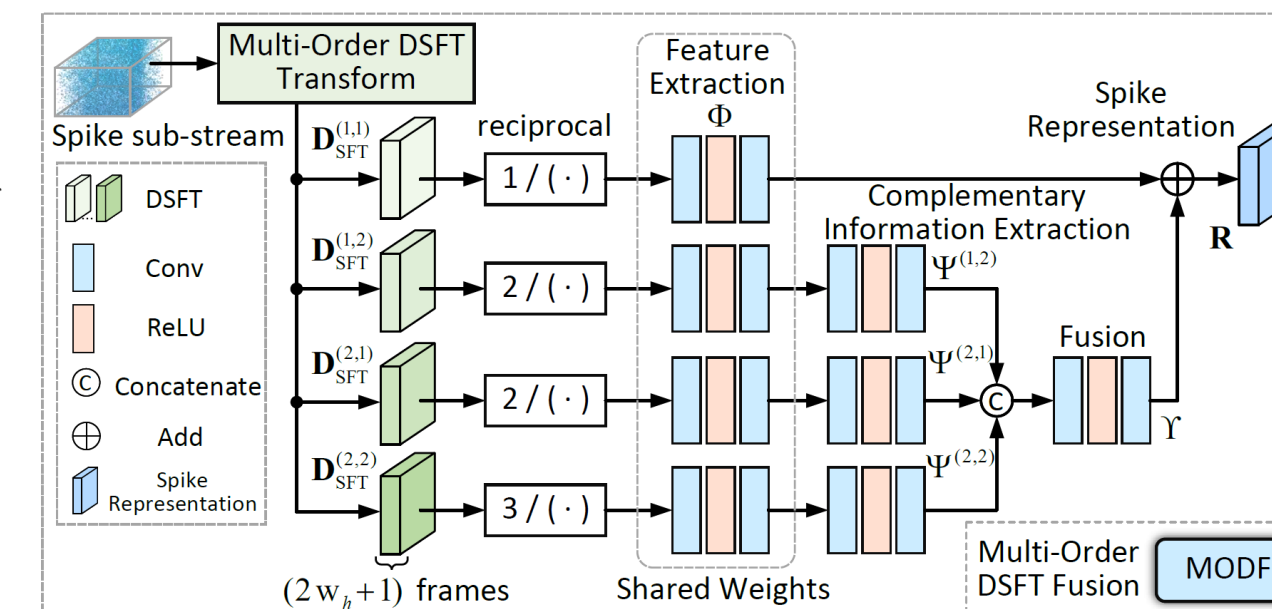
For reducing Poisson effects and light changes: purchase a more stable DSFT.

$$D_{SFT}^{(n_1, n_2)}(\mathbf{x}, t) = \mathbf{T}_{next}^{(n_2)}(\mathbf{x}, t) - \mathbf{T}_{prev}^{(n_1)}(\mathbf{x}, t)$$

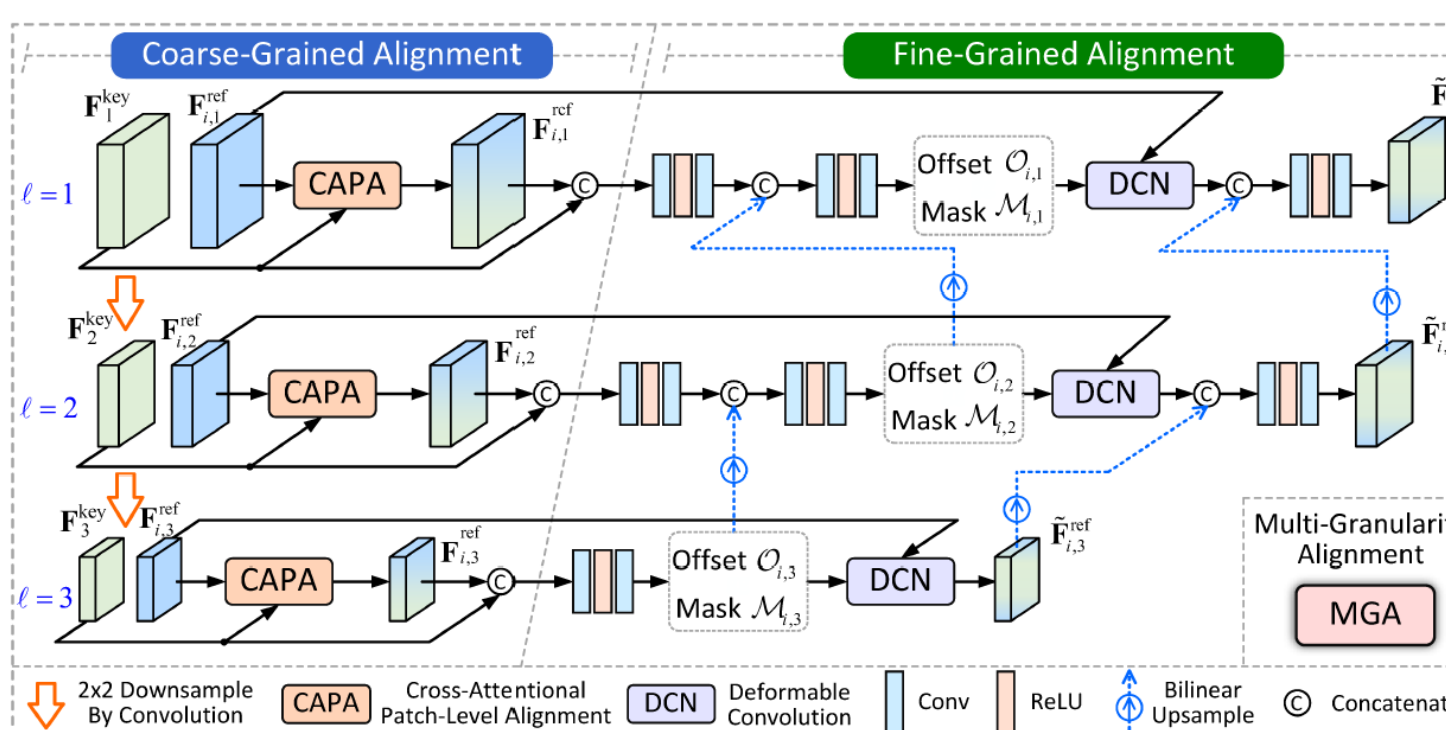
$$= \min\left\{\tau \mid \sum_{k=t+1}^{\tau} S(\mathbf{x}, k) = n_2, \tau > t\right\}$$

$$- \max\left\{\tau \mid \sum_{k=\tau}^t S(\mathbf{x}, k) = n_1, \tau \leq t\right\}$$

Structure of the multi-order DSFT fusion module based on the 3 propositions



2.3 Multi-Granularity Alignment (MGA)



Structure of the MGA module

Pyramidal structure

At each pyramidal level

First coarse-grained alignment

Then fine-grained alignment

(A) Coarse Grained Alignment: (CAPA) Cross-Attentional Patch-level Attention

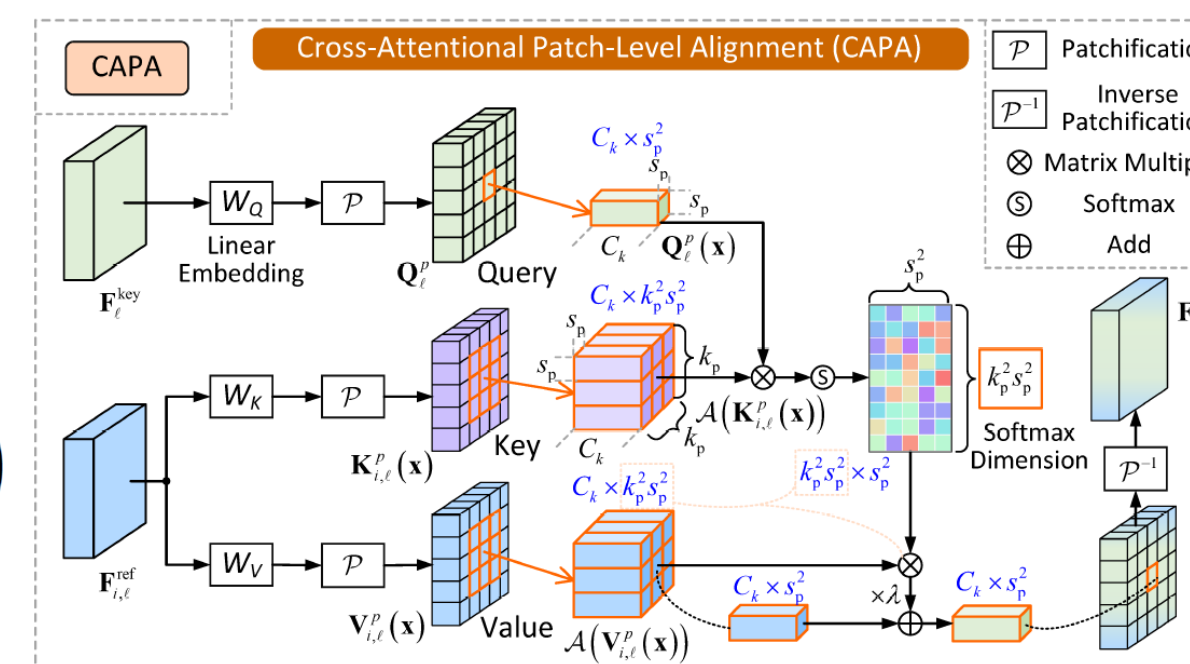
$$Q_\ell^p = \mathcal{Z}[Q_\ell] = \mathcal{Z}[W_Q F_\ell^{\text{key}}]$$

$$K_{i,\ell}^p = \mathcal{Z}[K_{i,\ell}] = \mathcal{Z}[W_K F_{i,\ell}^{\text{ref}}]$$

$$V_{i,\ell}^p = \mathcal{Z}[V_{i,\ell}] = \mathcal{Z}[W_V F_{i,\ell}^{\text{ref}}]$$

$$\hat{V}_{i,\ell}^p(\mathbf{x}) = \mathcal{A}(V_{i,\ell}^p(\mathbf{x})) \sigma\left(\frac{(Q_\ell^p)^\top(\mathbf{x}) \mathcal{A}(K_{i,\ell}^p(\mathbf{x}))}{\sqrt{C_k}}\right)$$

$$\mathcal{A}(V_{i,\ell}^p(\mathbf{x})) = \{V_{i,\ell}^p(\mathbf{x} + \delta)\}_{\delta \in \mathcal{N}(\mathbf{x}; k_p)}$$



(B) Fine Grained Alignment: Deformable Convolution

$$\tilde{F}_i^{\text{ref}}(\mathbf{x}) = \sum_{\delta \in \mathcal{N}(\mathbf{x}; k_d)} K(\delta) \hat{F}_i^{\text{ref}}(\mathbf{x} + \delta + O_i(\mathbf{x}, \delta)) \mathcal{M}_i(\mathbf{x}, \delta)$$

3. Experiments

3.1 Quantitative Results on REDS-SCIR Dataset

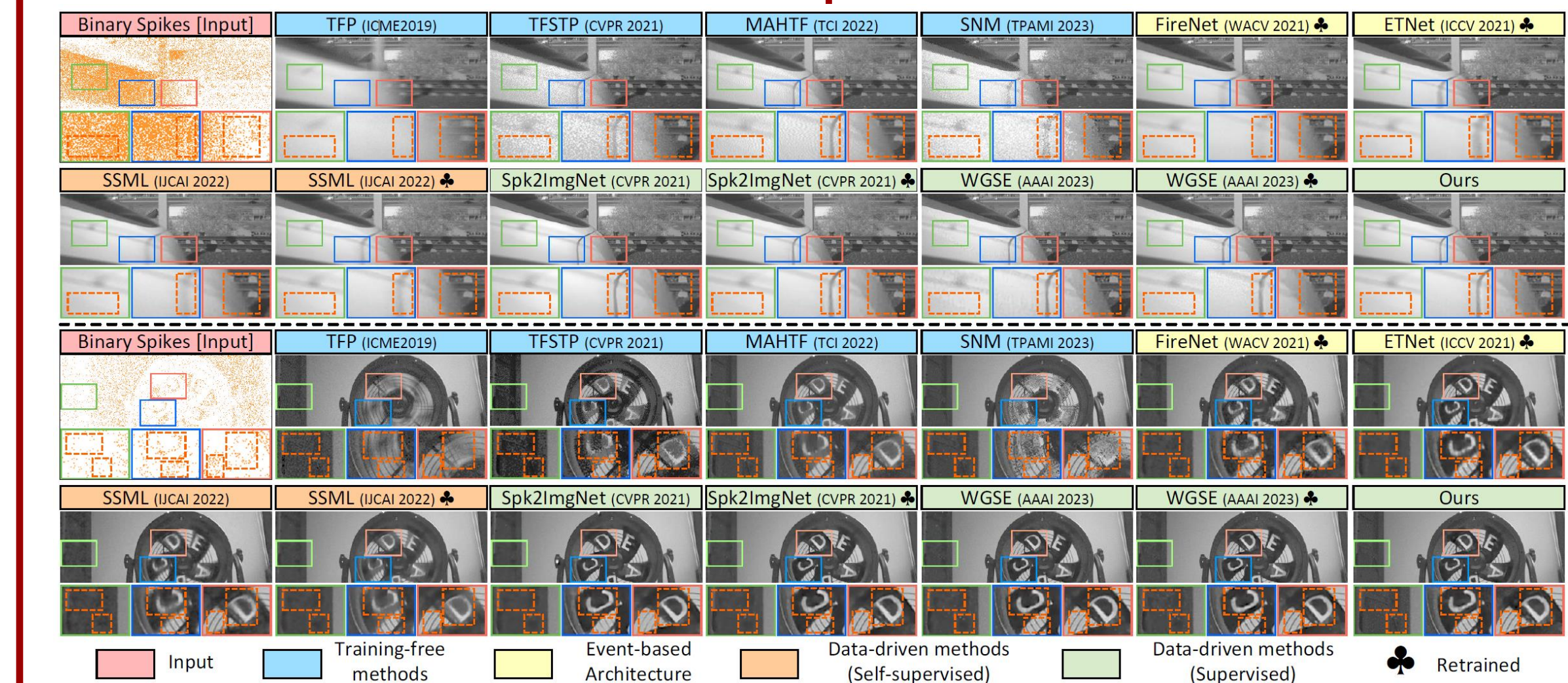
(1) Reference-based metrics

Part	Method	$\eta = 1.00$			$\eta = 0.75$			$\eta = 0.50$			Params (M)
		PSNR \uparrow	SSIM \uparrow	LPIPS \downarrow	PSNR \uparrow	SSIM \uparrow	LPIPS \downarrow	PSNR \uparrow	SSIM \uparrow	LPIPS \downarrow	
(A)	TFP [73]	27.27	0.711	0.265	26.73	0.669	0.300	25.62	0.581	0.370	—
	TFI [73]	23.55	0.634	0.329	24.77	0.673	0.293	26.77	0.713	0.249	—
	TFSTP [69]	20.35	0.678	0.270	19.62	0.685	0.252	21.10	0.707	0.247	—
	MAHTF [65]	29.57	0.879	0.112	30.07	0.884	0.113	29.65	0.869	0.136	—
(B)	FireNet [39] \clubsuit	34.38	0.922	0.077	33.87	0.911	0.084	32.62	0.884	0.105	0.038
	ETNet [46] \clubsuit	33.24	0.918	0.082	32.85	0.909	0.089	31.96	0.889	0.109	22.179
(C)	SSML [5]	32.60	0.920	0.088	32.09	0.907	0.097	31.00	0.879	0.122	2.385
	SSML [5] \clubsuit	33.94	0.923	0.075	33.27	0.909	0.088	32.01	0.883	0.116	2.385
(D)	Spk2ImgNet [64]	35.21	0.953	0.036	34.70	0.945	0.044	33.75	0.926	0.064	3.904
	Spk2ImgNet [64] \clubsuit	39.16	0.966	0.024	38.27	0.958	0.032	36.59	0.940	0.051	3.904
	WGSE [58]	35.21	0.950	0.039	34.98	0.947	0.042	34.11	0.931	0.057	3.806
	WGSE [58] \clubsuit	38.97	0.964	0.027	38.23	0.957	0.034	36.75	0.940	0.049	3.806
	BSF (Ours)	39.76	0.970	0.021	39.09	0.964	0.027	37.76	0.951	0.040	2.477

(2) Non-reference-based metrics

Part	Method	BRISQUE \downarrow	PIQE \downarrow	HOSA \downarrow	Part	Method	BRISQUE \downarrow	PIQE \downarrow	HOSA \downarrow
		37.502	45.956	35.436			(C)	SSML [5]	29.240
(A)	TFP [73]	37.708	45.148	30.892	(D)	SSML [5] \clubsuit	32.234	26.981	35.554
	TFI [73]	37.585	38.714	29.173		Spk2ImgNet [64]	29.351	26.745	25.761
	TFSTP [69]	32.089	41.927	29.334		Spk2ImgNet [64] \clubsuit	29.180	39.593	31.287
	SNM [75]	30.910	30.068	26.757		WGSE [58]	24.637	27.831	25.657
	MAHTF [65]	25.545	25.076	35.305		WGSE [58] \clubsuit	23.429	30.673	27.434
(B)	FireNet [39] \clubsuit	33.403	46.682	36.482	BSF (Ours)	18.529	23.477	25.523	

3.2 Visualization Results on Real-Captured Data



3.3 Ablation Studies

Ablations on Proposed Modules

Case	MODF	MGA			PSNR \uparrow		
		DCN	CAPA	Pym	$\eta = 1.00$	$\eta = 0.75$	$\eta = 0.50$
(1) Spike					38.44	37.69	36.29
(2) D (1,1)					38.78	38.10	36.80
(3)					38.99	38.32	37.00
(4)	\checkmark			1	38.91	38.26	36.96
(5)	\checkmark	\checkmark		1	39.06	38.39	37.06
(6)	\checkmark	\checkmark		2	39.02	38.39	37.11
(7)	\checkmark	\checkmark		2	39.39	38.73	37.41
(8)	\checkmark	\checkmark		3	39.38	38.77	37.53
(9)	\checkmark	\checkmark		3	39.76	39.09	37.76

Ablations on the number of input frames

N _{if}	$\eta = 1.00$			$\eta = 0.75$			$\eta = 0.50$		
	P \uparrow	S \uparrow	L \downarrow	P \uparrow	S \uparrow	L \downarrow	P \uparrow	S \uparrow	L \downarrow
21	38.14	0.959	0.032	37.44	0.952	0.039	36.08	0.935	0.055
41	39.35	0.969	0.021	38.67	0.963	0.027	37.34	0.949	0.041
61	39.76	0.970	0.021	39.09	0.964	0.027	37.76	0.951	0.040
81	39.70	0.969	0.022	39.03	0.963	0.028	37.69	0.950	0.042

Ablations on Hyper-parameters of the CAPA module

Pym	MGA			s_p	k_p	PSNR \uparrow		
	DCN	CAPA				$\eta = 1.00$	$\eta = 0.75$	$\eta = 0.50$
3	\checkmark	\times	\times	\times	39.380	38.768	37.533	
3	\checkmark	\times	\times	3	39.759	39.088	37.764	
3	\checkmark	\checkmark	\times	5	39.704	39.041	37.714	
3	\checkmark	\checkmark	\times	7	39.693	39.030	37.714	
3	\checkmark	\checkmark	\times	9	39.700	39.037	37.721	

Pym	MGA			s_p	k_p	PSNR \uparrow		
	DCN	CAPA				$\eta = 1.00$	$\eta = 0.75$	$\eta = 0.50$
3	\checkmark	\times	\times	\times	39.380	38.768	37.533	
3	\checkmark	\checkmark	\times	3	39.759	39.088	37.764	
3	\checkmark	\checkmark	\times	5	39.712	39.047	37.726	
3	\checkmark	\checkmark	\times	7	39.731	39.069	37.749	
3	\checkmark	\checkmark	\times	9	39.694	39.020	37.685	